

SPPU-BE-COMP-CONTENT - KSKA Git

DAA

classmate

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ASSIGNMENT-4.

Q1

Let

n = number of items

W = maximum weight capacity of the knapsack

dynamic programming approach builds a table $DP[n+1][W+1]$ where each entry represents the max value for a given weight & subset of items

Time Complexity:

$$O(n \times W)$$

\therefore we compute each DP cell once

Space Complexity:

$$O(n \times W)$$

if we optimise using 1D array then

$$O(W)$$

Q2

APPLICATIONS:

1) Budget Allocation / Investment Planning:

companies can decide how to allocate a fixed budget among multiple projects to maximise profit where each project has a cost (weight) & expected return (value)

2. Cargo Loading & Logistics:

used to determine which items to load into a container or truck with limited capacity to maximise total value without exceeding the weight limit.

Q3

| Item | Weight | Benefit |
|------|--------|---------|
| 0 | 2 | 3 |
| 1 | 2 | 7 |
| 2 | 4 | 2 |
| 3 | 5 | 9 |

Max wt (w) = 10

No. of items (n) = 4

Step 1: Initialise DP Table

We create table $K[n+1][w+1]$

where $K[i][w]$ = max benefit using first i items with capacity w

We fill it using above formula

$$K[i][w] = \begin{cases} 0 & \text{if } i = 0 \text{ or } w = 0 \\ K[i-1][w] & \text{if weight}[i-1] > w, \text{ else} \\ \max(K[i-1][w], \text{benefit}[i-1] + K[i-1][w - \text{weight}[i-1]]) & \end{cases}$$

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Step 2: Fill DP Table

- For each item & weight
- if item too heavy → use previous value
- else take max of including or excluding the item
- last cell = max benefit.

DP Table

| Item/ Capacity | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----------------|---|---|---|---|----|----|----|----|----|----|----|
| 0 | 0 | 0 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| 1 | 0 | 0 | 7 | 7 | 10 | 10 | 10 | 10 | 10 | 10 | 10 |
| 2 | 0 | 0 | 7 | 7 | 10 | 10 | 10 | 10 | 10 | 10 | 10 |
| 3 | 0 | 0 | 7 | 7 | 10 | 10 | 10 | 10 | 10 | 10 | 10 |

Max benefit = 19

Selected item S : 0, 1, 2 (Total Weight = 9)